

Adding Value through Risk Management in P&C

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Adding Value through Risk Management in P&C

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Extract from ECA2012* --



Solvency 2 ORSA : Three Approaches

Pillar 1 is main focus as it is tangible and immediate. Minimum compliance with ORSA.

Doing ERM because regulation requires it.

Not seen as a compliance exercise.

See ORSA as a proxy for a holistic ERM framework that benefits the insurer and adds value.

Not a function of firm size – more a function of senior management philosophy.

Pillar 1 Focussed

Compliance Focussed

Added Value Focussed

(*) Elliot Varnell – ERM and the challenges for actuarial consultants http://www.gcactuaries.org/documents/ECA2012 varnell.pdf





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Laws and Regulations: Solvency II

- Solvency II is the major European project on insurance legislation for the next few years. Solvency II will lead to a completely different Supervisory System as well as enhanced use of Risk capital models and Risk management systems.
- Solvency II is the new proposed EU legislation which will govern the capital requirements of insurance companies.
- The current Solvency Framework, Solvency I, was introduced in the early 70's and defined capital requirements by specifying simple, factor-based solvency margins, which did not always reflect the true risks in a given portfolio of insurance business.
- Solvency II is an opportunity to improve insurance regulation and supervision, introducing a risk based economic approach.



Main goals of Solvency II

- Risk based Solvency II calculations: incentive for integrated risk management
- Convergence issues:
 - to Basel II in Europe
 - of supervisory approaches
- Market consistent valuation of assets and liabilities
- Group Supervision
- Increased transparency concerning supervisory practice and the business model of insurance companies
- Common market place level playing field

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Solvency II: a Three-Pillar Structure



There are a lot of interdependencies between the different tasks within the different pillars



Purpose of the Risk Management

Putting all risks of a company on the scales ...



Capital consumption comes at a **cost** (reduces the value)

... the idea is to correctly balance them, in order to create value!!



Risk Capital

SCR.1.9 The SCR (Solvency Capital Requirement) should correspond to the Value-at-Risk of the basic own funds of an insurance undertaking subject to a confidence level of 99.5% over a one-year period



So, everything that affects the own funds in the next 12 months should be considered as a **risk**



Risk Capital

Step 1: Assessment of nature, scale and complexity of risks

SCR.1.19 The insurer should assess the **nature**, **scale** and **complexity** of the risks [...]

Step 2: Assessment of the model error

SCR.1.21 Where simplified approaches are used to calculate the SCR, this could introduce **additional estimation uncertainty** (or **model error**) [...]

SCR.1.23 Undertaking **are not required to quantify** the degree of **model error** in **quantitative terms** [...] Instead, it is sufficient **if there is reasonable assurance that the model error included in the simplifications is immaterial**

All the uncertainty – except of model error - should be considered in quantitative terms. This means that parameter and process error are in scope.



Risk Capital

Being the risk represented by the uncertainty of the future NAV development, this can be split into several categories, corresponding to the events giving place to the possible NAV variations



Risks Universe

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Reserve Risk

SCR.9.11 Reserve risk results from *fluctuations* in the *timing* and *amount* of *claim settlement*



In order words, it's like if we simulate the fact we are at the end of the reserve run-off and we observe how wrong we were at the instant of evaluation



Reserve Risk

Tons of studies in actuarial literature regarding the Stochastic Loss Reserving





Reserve Risk – The underlying models

There is a "change of perspective" compared with the past

DETERMINISTIC MODELS









Reserve Risk – The underlying models

In order to use stochastic model, you need to fix stochastic assumptions

Assumptions		Example
PARAMETRIC	Give the parametric distribution family of ${\it P}_{\!$	GLM
SEMIPARAMETRIC	Give only some assumptions on some moments	ODP / MACK

Usually the market is now considering **massively** only two stochastic models (ODP model & Mack model), and they are also generally accepted by Solvency II directive





Reserve Risk – The underlying models



To do a correct bootstrap exercise, an analysis on residuals must be performed (they must be i.i.d) => **Residuals Analysis**



Reserve Risk - Shift to actuarial reserves

The implied expected value when assessing reserving uncertainty **does not necessarily correspond** to the best estimate reserve set by the Reserving Actuary (often based on different deterministic methods). However, we are still interested in the predictive distribution around the best estimate selected by the Reserving Actuary.



Generally, the common idea is to stay always on the safe side choosing a prudential approach (e.g. if ABE > BE then **multiplicative**, else **additive**)



Reserve Risk - Where are the problems?

Let's give a look again to the definition of SCR

SCR.1.9 The SCR (Solvency Capital Requirement) should correspond to the **Value-at-Risk** of the **basic own funds** of an insurance undertaking subject to a confidence level of 99.5% over a <u>one-year period</u>

So, in 2008, the IAIS(*) published the following interpretation:

"[...]

- Shock period: the period over which a shock is applied to a risk;
- *Effect horizon*: the period over which the shock that is applied to a risk will impact the insurer

In essence, at the end of the shock period, capital has to be sufficient so that assets cover the technical provision (...) **re-determined at the end of the shock period**. The re-determination of the technical provisions would allow for the impact of the shock on the technical provisions over the full time horizon of the policy obligations"

^(*) International Association of International Supervisors

Guidance paper No. 2.1.1 on the structure of regulatory capital requirements (October 2008), Art. 55

http://www.iaisweb.org/view/element_href.cfm?src=1/5778.pdf

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All the models seen until now consider a "shock" until the full reserve run-off (the so called "**Ultimate View**")





Reserve Risk - The "1yr View"

From 2008, only two main studies have been performed on the topic

Merz, Wuthrich (June 2008) - Modelling the Claims Development Result for Solvency Purposes (ASTIN)

- Based on Mack (1993) assumptions + additional assumptions (martingale process)
- No tails considered
- Closed form for MSEP calculation (no information on the tails)
- Consider both a "perspective" and retrospective view

Starting from QIS5 it has been officially recognized for the calculation of the USP (Undertaking Specific Parameters), to be used thru a credibility approach with the market parameters



Reserve Risk - The "1yr View"

Ohlsson, Esbjorn, Lauzeningks (2008) - The one-year non-life insurance risk

Gives only the general idea on how the one-year view should be evaluated (i.e. implementing the **re-reserving algorithm** – the so called "actuary in the box")
If we consider as re-reserving algorithm only the CL, we get the previous Merz-Wuthrich approach



This approach is particular interesting for the internal model implementation; anyway, in these last years, not many studies in actuarial literature have been done: **there are still a lot of open issues to be deepen**



Reserve Risk - In a nutshell

The "**Ultimate View**" it has been commonly understood and accepted, but – practically – relies still too much to "CL-centered" models

On the contrary, "**1yr View**" has still lot of interpretational issues and more studies have to be performed



Anyway, at the moment, the main "quantitative" issues are more or less solved and received a positive feedback from QIS5 exercise



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Premium Risk

SCR 9.9. Premium risk results from fluctuations in the timing, frequency and severity of insured events. **Premium risk** relates to **policies to be written** (**including renewals**) during the period, and **to unexpired risks on existing contracts**. Premium risk includes the risk that **premium provisions** turn out to be **insufficient** to compensate claims or need to be increased.

It's an "atypical" risk, since it involves mainly P&L quantities (i.e. the future profit/losses) other than b/s figures (i.e. the Unearned Premium Reserve)

Basically, it's a shock on the combined ratio for a given volume measure

$$RC = \left(CoR_{WC(99.5\%)} - CoR_{BE}\right) \cdot V_{(prem, lob)}$$



Premium Risk – Evaluating the "CoR shock"

 $(CoR_{WC(99.5\%)} - CoR_{BE})$

The **shock** is – more or less – quite easy to assess, typically based on historical CoR series:

- What about Premium Cycle uncertainty? It's very difficult to assess its uncertainty
- Doing so far, are we considering an "ultimate" or a "1-yr view" ?
- And should we consider a correlation between losses and premiums "embedded" in the CoR?
- How to evaluate the impact of the Reinsurance structure?

Internal models often do a complete stochastic modeling (via a Montecarlo approach), useful also for other purposes (see Reinsurance Optimisation) ... BUT ...



Premium Risk – The volume measure



denotes the expected present value of premiums to be earned by the insurance undertaking in the segment s for contracts where the initial recognition date falls in the following 12 months but excluding the premiums to be earned during the 12 months **after the initial recognition date**

 $FP_{(future,s)}$



Premium Risk – The volume measure

... and it still have some issues ©

Take for example a 2 years policy, with a single premium of 2.000€, that will incept in the middle of next year

The earnings of the contract as described the S2 volume measure are:



Reminder: FP_(future,s) denotes the expected present value of premiums to be earned by the insurance undertaking in the segment s for contracts where the initial recognition date falls in the following 12 months but excluding the premiums to be earned during the 12 months **after the initial recognition date (**it should say **"after the next 12 months"**!!!)



Premium Risk - In a nutshell

Still not clear the perimeter of the Premium Risk, but it's mainly related to earned premiums and UPR revaluation after one-year (why don't call this latter *"Premium Reserve" Risk?*)

Other minor issues due to Premium Cycle interpretation and assumptions to be considered ...



But the real problem regards **data quality and availability**: in the past data of future premiums have not been used in the balance sheet



Nat-Cat Risk – A quick overview

• "Natural catastrophe" ("Nat Cat") is a damaging event produced by nature elements followed by several single losses, involving a number of contracts (and then a number of contracting parties)

• The **extent** of a natural catastrophe depends on the force of the natural agent itself, but also on **man-made factors**, such as the quality of preventive measures adopted in the considered area, the technical building features, the maintenance level

- This risk includes:
 - Earthquakes (including seaquakes and tsunami)
 - Flood
 - Hail
 - Hurricane, storm, avalanches, snow and freeze

Usually, on a gross basis, the Nat-Cat risk "consume" a lot of capital ...



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1 - Introduction

The idea of Risk Aggregation



We can calculate the standalone RC_i applying a **risk measure** $\rho(.)$ to each $X_1, ..., X_n$. The total risk capital is calculated applying the same risk measure to the distribution function of *X*.



1 - Introduction

The idea of Capital Reallocation



Once we have the total risk capital (that takes into account dependencies and diversification effect), we want to re-allocate this figure to the single risks.

One of the main aims of Capital Reallocation is to compute the Cost of Capital relative to single risks/LoBs, in order to **determine risk adjusted profitability of single segments.**



2 - Risk Measures

Definition of **Risk Measure**

In actuarial literature, a risk measure is defined as a mapping ρ from a set *L* of real-valued random variables defined on a probability space (Ω , ζ , λ) to the real line R:

$$\rho: L \to \mathbb{R}$$

i.e. $\rho: X \in L \to \rho(X)$

Usually, if X represents a random return, from an economic point of view we can see $\rho(X)$ as the (<u>positive</u>) **amount of capital** set aside in order to make X an acceptable risk (*)

(*) Generally the concept of setting aside a Risk Capital to hedge the risks is a direct consequence of the "translation invariance" property (see slide 9), i.e. setting aside a Risk Capital that equals $\rho(X)$ makes the total risk measure go to zero.



2 - Risk Measures

Definition of Coherent Risk Measure

A risk measure *ρ* is called *coherent* if it satisfies the following properties ([1] Artz et. al. (1999)):

- (*i*) Translation Invariance: $\rho(X + \alpha) = \rho(X) \alpha, \forall X \in L, \alpha \in \mathbb{R}$
- (*ii*) Subadditivity: $\rho(X+Y) \le \rho(X) + \rho(Y), \forall X, Y \in L$
- (*iii*) Positive Homogeneity: $\rho(\beta X) = \beta \rho(X), \forall X \in L, \beta \ge 0$
- (*iv*) Monotonicity: $\rho(X) \le \rho(Y)$, $\forall X, Y \in L$ with $X \ge Y \lambda$ -a.s.

These properties are desirable because they all have an interpretation that is logical from an economic point of view (e.g. without the Subadditivity, the risk measure can show <u>anti-diversification</u>)



2 - Risk Measures

Some well-known Risk Measures:

(*i*) Variance: $\rho_{var}(X) = var(X)$ (*ii*) Standard deviation: $\rho_{sd}(X) = \sigma(X) = \sqrt{var(X)}$ (*iii*) Value-at-Risk (VaR): $\rho_{VaR(\alpha)}(X) = -VaR_{(\alpha)}(X)$ (*iv*) TVaR¹: $\rho_{TVaR(\alpha)}(X) = -E(X | X \le VaR_{(\alpha)}(X))$

Please note that in this case α is a 'left-side' number, e.g. 0.5% for Solvency II

Among these, only the TVaR is a **coherent** risk measures.

1. In our assumptions the underlying distribution is continuous, therefore the TVaR (also called Tail Conditional Expectation) is the same as the Expected Shortfall ([2] Acerbi, Tasche (2002)).



3 - Allocation Methods

Definition of Allocation Method

We denote by M the set of risk measures. A capital allocation method Φ is a mapping

$$\Phi: M \times L^n \to \mathbb{R}^n, \quad (\rho, X_1, \dots, X_n) \to \begin{pmatrix} \Phi_1(\rho, X_1, \dots, X_n) \\ \dots \\ \Phi_n(\rho, X_1, \dots, X_n) \end{pmatrix}$$

Therefore, an allocation method is defined once we choose a **particular** form for the functional Φ .


From now on we will use the following notation:

- $\rho(X)$ for the risk capital allocated to the total portfolio
- $\rho(X_i)$ for the standalone risk capital allocated to the single risk
- $\rho(X_i|X)$ for the contributory risk capital reallocated to the single risk

Besides, we can briefly introduce the concept of Return On Risk Adjusted Capital (**RORAC**):

• related to the total (*):
$$RORAC(X) = \frac{E(X)}{RC_{TOT}} = \frac{\sum_{i=1}^{n} \mu_i}{\rho(X)}$$

• related to the single contribution (*): $RORAC(X_i) = \frac{E(X_i)}{RC_i} = \frac{\mu_i}{\rho(X_i \mid X)}$

(*) Please note that in this notation $\rho(X) = RC$, e.g. $\rho(X) = [-VaR_a(X)] - E(X)$

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"Definition" of **Coherent Allocation Method**, and economic reasons on why we should look for a coherent allocation method

(*i*) Full allocation property:
$$\sum_{i=1}^{n} \rho(X_i | X) = \rho(X).$$

<u>comment</u>: it is obvious that we need the single contributory risk capitals to add up to the total risk capital. By the way, this condition is easy to obtain just by putting some constraints on the coefficients Φ_i

(*ii*) Diversifying allocation property: $\rho(X_i | X) \le \rho(X_i)$, i = 1, ..., n

<u>comment</u>: we clearly want to take diversification into account when reallocating risk capital to the single risks/Lobs



(*iii*) RORAC compatibility property: $RORAC(X_i | X) > RORAC(X) \implies RORAC(X + hX_i) > RORAC(X)$ for all h > 0, i = 1,...,n

<u>comment</u>: without this property the reallocation process results could be economically odd

These properties are desirable because they all have an interpretation that is logical from an economic point of view. It is reasonable to look for allocation methods that verify them.

OSS: Generally speaking **there is no reason to impose non-negative coefficients** (e.g. to allow for hedging effects) (*)

(*) Please note that there is no allocation method that always verify the non-negativity, but we may need it if we want to use RAPM-type quotients (return/allocated capital); see [4] Denault (2001) for an insight on the non-negativity property for reallocation methods



Examples of Allocation Principles

(*i*) Proportional:
$$\Phi_i^{P,\rho} = \rho(X_i) / \sum_{j=1}^n \rho(X_j)$$

(*ii*) Marginal Approach (or Merton & Perold): $\Phi_i^{MP,\rho} = \frac{\rho(X) - \rho(X - X_i)}{\sum_{j=1}^n \left[\rho(X) - \rho(X - X_j)\right]}$

(*iii*) Euler Allocation (or Myers & Read):
$$\Phi_i^{Eu,\rho} = \frac{\partial \rho(X)}{\partial u_i} / \sum_{j=1}^n \frac{\partial \rho(X)}{\partial u_j}$$

It is shown in the actuarial literature that only the Euler Allocation applied to a coherent risk measure can be a coherent allocation method

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How to build a Capital Reallocation Approach

As we've seen, we can write:

$$RC_{i} = \Phi_{i} \cdot RC_{TOT} = \frac{\rho^{a}(X_{i} \mid X)}{\sum_{i=1}^{n} \rho^{a}(X_{i} \mid X)} \cdot \rho^{TOT}(X)$$

Therefore, to fully describe the allocation approach we need to define:

- $\bullet\,\Phi$ is the function that describes the **allocation principle**
- ρ^a is the risk measure used inside the functional Φ
- ρ^{TOT} is the risk measure used to obtain the total risk capital

In the actuarial literature ρ^a and ρ^{TOT} are always the same, since this is required to have some good properties verified. In the practice they are often different.



"Standalone Approach"

Allocation principle (Φ)	Risk measure for re-allocation (<i>p</i> ^a)	Risk measure for total RC ($ ho^{ extsf{TOT}}$)
Proportional	Usually VaR or TVaR	Usually VaR or TVaR

PRO

· Very easy to calculate

CONS

• Does not take into account intra-risks diversification benefit, and **this is true for every risk measure we choose**



"Marginal Approach"

Allocation principle (Φ)	Risk measure for re-allocation (<i>p</i> ^a)	Risk measure for total RC ($ ho^{ extsf{TOT}}$)
Marginal	Usually VaR	Usually VaR
(Merton & Perold)	or TVaR	or TVaR

PRO

• "What if" point of view

CONS

· Computational demanding, we need the joint distribution of $(X - X_i)$ for every i

• For any risk measure, **it is not a coherent allocation method** ([11] Tasche (2007))

This method may be useful to analyse the impact of adding/removing one entire LoB, but it is not suited to reallocate the Cost of Capital



"Covariance Approach"

Allocation principle (Φ)	Risk measure for re-allocation (<i>p</i> ^a)	Risk measure for total RC ($ ho^{ extsf{TOT}}$)
Euler (Myers & Read)	Standard deviation	Usually VaR or TVaR

This could be a coherent allocation method, but only if we use the **standard deviation** for <u>**both**</u> ρ^{a} and ρ^{TOT} . Please note that the standard deviation could be a coherent risk measure under more restrictive assumptions.

If we want to use the VaR or TVaR for computing the total Risk Capital, then this is not a coherent allocation method (*[10] Tasche (2004*), p.14)



"Decomp VaR Approach"

Allocation principle (Φ)	Risk measure for re-allocation (<i>p</i> ^a)	Risk measure for total RC ($ ho^{ extsf{TOT}}$)
Euler (Myers & Read)	VaR	Usually VaR or TVaR

PRO

· Very easy to calculate

CONS

· Very unstable, and not a reliable measure of risk contributions



"VaR HD"

Allocation principle (Φ)	Risk measure for re-allocation (<i>p</i> ^a)	Risk measure for total RC ($ ho^{ extsf{TOT}}$)
Euler (Myers & Read)	VaR HD	Usually VaR (HD) or TVaR

PRO

· "Decent" representation of risk contributions

CONS

· It is not a coherent capital allocation method, therefore it can sometimes give odds results



"Contribution to TVaR Approach"

Allocation principle (Φ)	Risk measure for re-allocation ($ ho^{a}$)	Risk measure for total RC ($ ho^{ extsf{TOT}}$)
Euler (Myers & Read)	TVaR	Usually VaR or TVaR

It's possible to prove that if we use the **TVaR to measure the total risk** capital and to reallocate, then we have a coherent allocation method with a coherent risk measure (*TVaR*) - ([10] Tasche (2004) and [11] *Tasche (2007)*)



In fact, following this proposal we obtain:



PROs	
1. We use a coherent risk measure to calculate the total risk capital	\checkmark
2. We use a coherent capital allocation method	\checkmark
3. It is very easy to calculate the single contributions (see next)	\checkmark
4. it uses all the information from both the total distribution and the marginal distributions	\checkmark
5. It can be used for different economic purposes just by changing the α (i.e. if we want a risk management approach we can focus on the tails with α =0.5%, if we want a more "expected" approach we can set α =50%)	\checkmark

CONs	
It doesn't work for non-linear risks (e.g. Market Risks)	X
The TVaR requires at least 10'000 sims at the 99% confidence level to give stable results ([13] Yamai, Yoshiba (2007))	X



5 - Reallocation in Practice

Initial assumptions:

- We know (or have estimated) the marginal distributions
- We know (or have estimated) the copula that describes the dependencies
- We can simulate *n* values from each marginal
- We can apply the dependency described by the copula through a reordering algorithm



We have *n* scenarios for the Total P&L, with all the information about the marginals that created those scenarios



5 - Reallocation of Risk Capital in practice

1	TOTAL	CREDIT			PREI	M NONCAT	PREM NATCAT				TC	CREDIT			PREM NONCAT		PREM NATCAT			
Base Sc	enario Total	Base Sce	nario		Base So	cenario	Base Sc	cenario			Base Scer	nario Total	Base So	enario	1	Base Sc	Base S	cenari)	
MC 1	- 389,383	MC_1	- 2	2,349	MC_1	- 284,997	MC_1	-	24,394		MC_9	-1,770,874	MC_9	-	82,055	MC_9	- 330,36	7 MC_9	-	12,234
MC ⁻ 2	66,649	MC 2	4	,539	MC ²	217,133	MC ⁻ 2		21,487		MC_31	-1,232,559	MC_31	-	65,327	MC_31	- 213,58	6 MC_31	-	26,133
мстз	444,444	мстз	7	491	мс з	66,689	мс з		5,481		MC_42	- 780,867	MC_42	-	31,870	MC_42	109,57	7 MC_42	-	80,510
MC_4	407,828	MC_4	6	507	MC_4	- 173,492	MC_4		11,180		MC_26	- 769,784	MC_26		1,587	MC_26	- 179,75	9 MC_26		15,845
MC_5	185,757	мс 5	-	381	MC_5	- 73,747	MC_5	-	23,569		MC_17	- 620,535	MC_17	-	12,189	MC_17	- 103,33	I MC_17	-	578
MC 6	- 573.607	MC 6	- 13	173	MC 6	147 894	MC 6	-	48 744		MC_6	- 573,607	MC_6	-	13,173	MC_6	147,89	4 MC_6	-	48,744
MC 7	93 736	MC 7	3	555	MC 7	86 124	MC 7		13 541		MC_30	- 554,817	MC_30	-	381	MC_30	- 106,31	5 MC_30		15,249
MC 8	- 146 126	MC 8	- 3	333	MC 8	82,130	MC 8	-	30,636		MC_38	- 420,353	MC_38		4,539	MC_38	- 15,99	2 MC_38	-	14,597
MC 9	-1 770 874	MC 9	- 82	055	MC 9	- 330 367	MC 9		12 234		MC_1	- 389,383	MC_1	-	2,349	MC_1	- 284,99	7 MC_1	-	24,394
MC_10	- 291 491	MC 10	4	1,539	MC_10	- 390,677	MC_10		17 539		MC_11	- 371,803	MC_11	-	13,173	MC_11	- 20,01	B MC_11	-	30,749
MC_11	- 371,401	MC 11	. 13	173	MC 11	- 000,077	MC 11	_	30.749		MC_19	- 352,858	MC_19		7,491	MC_19	- 201,35	2 MC_19		18,581
MC 12	135 088	MC 12	- 10	587	MC 12	30/ 8/2	MC 12	_	6347		MC_10	- 291,491	MC_10		4,539	MC_10	- 390,67	7 MC_10		17,539
MC 12	446 602	MC 12	4	,007	MC 12	1004,042	MC 12	-	10,047		MC_23	- 289,611	MC_23	-	9,237	MC_23	128,03	2 MC_23	-	12,162
MC_1J	440,000	MC_14	4	1/200	MC_13	210,001	MC_14	-	10,303		MC_40	- 230,699	MC_40		3,555	MC_40	190,23	8 MC_40	-	7,398
MC_14	790,223		9	404	NIC_14	340,323 475,504	MO_14		15,415		MC_8	- 146,126	MC_8	-	3,333	MC_8	82,13) MC_8	-	30,636
IVIC_15	652,424			,491	NIC_15	175,594	IVIC_15	-	32,936		MC_32	- 142,095	MC_32		1,587	MC_32	- 253,17	6 MC_32	-	30,569
MC_16	1,194,650		9	459	MC_16	196,472	MC_16	-	19,309		MC_34	- 96,648	MC_34		1,587	MC_34	- 213,49) MC_34		11,117
MC_17	- 620,535	MC_17	- 12	2,189	MC_17	- 103,331	MC_17	-	5/8		7 C_44	- 58,980	MC_44		2,571	MC_44	126,18	8 MC_44	-	12,032
MC_18	206,989	MC_18	5	6,523	MC_18	172,769	MC_18		7,663		MC_22	- 24,103	MC_22	-	4,317	MC_22	213,09	6 MC_22	-	53,112
MC_19	- 352,858	MC_19		,491	MC_19	- 201,352	MC_19		18,581		MC_35	- 17,751	MC_35		3,555	MC_35	84,25	7 MC_35	-	6,160
MC_20	421,706	MC_20	1	,587	MC_20	146,941	MC_20	-	9,109		MC_29	10,713	MC_29		603	MC_29	- 234,24	6 MC_29	-	18,798
MC_21	94,541	MC_21	7	′,491	MC_21	21,552	MC_21		11,711		MC_2	66,649	MC_2		4,539	MC_2	217,13	3 MC_2		21,487
MC_22	- 24,103	MO_22	- 4	,317	MC_22	213,096	MC_22	-	53,112		MC_7	93,736	MC_7		3,555	MC_7	86,12	4 MC_7		13,541
MC_23	- 289,611	MC_23	- 9	1,237	MC_23	128,032	MC_23	-	12,162		MC_21	94,541	MC_21		7,491	MC_21	21,55	2 MC_21		11,711
MC_24	116,418	MC_24		381	MC_24	255,703	MC_24	-	21,580		MC_24	116,418	MC_24	-	381	MC_24	255,70	3 MC_24	-	21,580
MC_25	516,682	MC_25	6	507	MC_25	139,504	MC_25		24,488		MC_12	135,088	MC_12		1,587	MC_12	304,84	2 MC_12	-	6,347
MC_26	- 769,784	MC_26	1	,587	MC_26	- 179,759	MC_26		15,845		MC_36	135,934	MC_36		4,539	MC_36	99,60	1 MC_36		4,951
MC_27	269,004	MC_27	4	,539	MC_27	- 243,404	MC_27		14,115		MC_5	185,757	MC_5	-	381	MC_5	- /3,/4	MC_5	-	23,569
MC_28	760,991	MC_28	9	9,459	MC 28	86,041	MC_28		11,891		MC_18	206,989	MC_18		5,523	MC_18	1/2,/6	9 MC_18		7,663
MC 29	10,713	MC 29		603	MC 29	- 234,246	MC 29	-	18,798		MC_27	269,004	MC_27		4,539	MC_27	- 243,40	1 MC_27		14,115
MC_30	- 554,817	MC 30	-	381	MC_30	- 106,315	MC_30		15,249		MC_43	347,359	MC_43		8,475	MC_43	- 9,98	I MC_43		517
MC_31	-1,232,559	MC_31	- 65	5,327	MC_31	- 213,586	MC_31	-	26,133		MC_39	357,940	MC_39		7,491	MC_39	49,98	5 MC_39		22,547
MC_32	- 142.095	MC 32	1	.587	MC_32	- 253,176	MC 32	-	30,569		MC_45	376,026	MC_45		7,491	MC_45	- 6,83	9 MC_45	-	6,385
мс зз	796.201	мства	10		MC_33	329,991	MC 33		25,961	1	MC_4	407,828	MC_4		6,507	MC_4	- 173,49	2 MC_4		11,180
MC 34	- 96.648	MC 34	1	587	MC 34	- 213,490					MC 20	421.706			1,587	MC_2U	146,94	I MC_20	-	9,109
MC 35	- 17 751	MC 35	3	555	MC 35	84 257			1	ton. C					7,491	IVIC_3	00,00	1 IVIC_3		5,481
MC 36	135 934	MC 36	4	1539	MC_36	99,604	1 5		5T 8	бтер: г	keol	raer	13		4,539	MC_13	160,31	2 MC_13	-	16,983
MC 37	670 321	MC 37	9	1/159	MC_37	195 116							-25		6,507	MC_25	139,50	1 IVIC_25		24,488
MC 38	- 420,353	MC 38	1	1639	MC 38	- 15 992	I T/			0000	oria				7,491	IVIC_15	175,59	1 IVIC_15	-	32,936
MC_30	357 940	MC 30	7	//01	MC 30	49,002 19,002		UI	AL	_ Scen	a n C	JS II	-37		9,459	IVIC_37	195,11	D IVIC_37		15,467
MC 40	- 230 699		2	101	MC 40	190,000	1								a sea	530 AB	86 10	. KAL AR		. Faul
MC_40	974 739		ر ار	1,530	MC 41	3/9 1/7		rd	lor	to find	d 14/	oret								
	-124 7 14		-			· A -(H)		U I				UI 3 L								
							1													
							1			ones										
										01163			100 100							



5 - Covariance Approach in practice var(X)



 $\Phi_{i} = \operatorname{cov}(X_{i}, X) / \operatorname{var}(X)$

TOTAL	Γ	с	REDIT	-		PREM	NO	NCAT	PREN		CAT
Base Scenario Total	E	lase Sc	enario			Base Sce	enari	o	Base Sci	enario)
MC_9 -1,770,874	1	4C_9	-	82,05	5	MC_9	-	330,367	MC_9	-	12,234
MC_31 -1,232,559	1	4C_31	-	65,32	7	MC_31	-	213,586	MC_31	-	26,133
MC_42 - 780,867	1	4C_42	-	31,87	þ	MC_42		109,577	MC_42	-	80,510
MC_26 - 769,784	1	4C_26		1,58	7	MC_26	-	179,759	MC_26		15,845
MC_17 - 620,535	1	4C_17	-	12,18	9	MC_17	-	103,331	MC_17	-	578
MC_6 - 573,607	1	4C_6	-	13,17	З	MC_6		147,894	MC_6	-	48,744
MC_30 - 554,817	1	4C_30	-	- 38	1	MC_30	-	106,315	MC_30		15,249
MC_38 - 420,353	1	4C_38		4,53	Э	MC_38	-	15,992	MC_38	-	14,597
MC_1 - 389,383	1	4C_1	-	2,34	Э	MC_1	-	284,997	MC_1	-	24,394
MC_11 - 371,803	1	4C_11	-	13,17	В	MC_11	-	20,013	MC_11	-	30,749
MC_19 - 352,858	1	4C_19		7,49	1	MC_19	-	201,352	MC_19		18,581
MC_10 - 291,491	1	4C_10		4,53	9	MC_10	-	390,677	MC_10		17,539
MC_23 - 289,611	1	4C_23	-	9,23	7	MC_23		128,032	MC_23	-	12,162
MC_40 - 230,699	1	4C_40		3,55	5	MC_40		190,233	MC_40	-	7,398
MC_8 - 146,126	1	4C_8	-	3,33	З	MC_8		82,130	MC_8	-	30,636
MC_32 - 142,095	1	4C_32		1,58	7	MC_32	-	253,176	MC_32	-	30,569
MC_34 - 96,648	1	4C_34		1,58	7	MC_34	-	213,490	MC_34		11,117
MC_44 - 58,980	1	4C_44		2,57	1	MC_44		126,183	MC_44	-	12,032
MC_22 - 24,103	1	4C_22	-	4,31	7	MC_22		213,096	MC_22	-	53,112
MC_35 - 17,751	1	4C_35		3,55	5	MC_35		84,257	MC_35	-	6,160
MC_29 10,713	1	4C_29		60	3	MC_29	-	234,246	MC_29	-	18,798

 $cov(X_i, X)$

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5 - Decomp VaR Approach in practice

т0	TAL	C	Г	PREM	I NO	NCAT	PREM NATCAT				
Base Scen	ario Total	Base Sc	enario	I	Base Sc	enar	io	Base Sc	enario)	
MC_9	-1,770,874	MC_9	-	82,055	MC_9	-	330,367	MC_9	-	12,234	
MC_31	-1,232,559	MC_31	-	65,327	MC_31	-	213,586	MC_31	-	26,133	
MC_42	- 780,867	MC_42	-	31,870	MC_42		109,577	MC_42	-	80,510	
MC_26	- 769,784	MC_26		1,587	MC_26	-	179,759	MC_26		15,845	
MC_17	- 620,535	MC_17	-	12,189	MC_17	-	103,331	MC_17	-	578	
MC_6	- 573,607	MC_6	-	13,173	MC_6		147 ,894	MC_6	-	48,744	
MC_30	- 554,817	MC_30	-	381	MC_30	-	106,315	MC_30		15,249	
MC_38	- 420,353	MC_38		4,539	MC_38	-	15,992	MC_38	-	14,597	
MC_1	- 389,383	MC_1	-	2,349	MC_1	-	284,997	MC_1	-	24,394	
MC_11	- 371,803	MC_11	-	13,173	MC_11	-	20,013	MC_11	-	30,749	
MC_19	- 352,858	MC_19		7,491	MC_19	-	201,352	MC_19		18,581	
MC_1U	- 291,491	4C_10		4,539	MIC_10	-	390,677	NIC_10		17,539	
MC_23	- 289,611	MC_23	-	9,237	MC_23		128,032	NIC_23	-	12,162	
MC 48	- 238,699	<u> 1/10_48</u>		3,555	MC 48		198,233	NC_48	-	7,398	
MC_8	- 146,126	MC_8	-	3,333	MC_8	1	82,130	MC_8	-	30,636	
MC_32	- 142,095	MC_32		1,587	MC_32	ł	253,176	MC_32	-	30,569	
MC_34	- 96,648	MC_34		1,587	MC_34	- 1	213,490	MC_34		11,117	
MC_44	- 58,980	MC_44		2,571	MC_44		126,183	MC_44	-	12,032	
MC_22	- 24,103	MC_22	-	4,317	MC_22		213,096	MC_22	-	53,112	
MC_35	- 17,751	MC_35		3,555	MC_35		84,257	MC_35	-	6,160	
MC_29	10,713	MC_29		603	MC_29	-	234,246	MC_29	-	18,798	
	¥						ł				
	VaR	?(X)		DecompVaR(X _i)							

 $\Phi_{i} = DecompVaR(X_{i}) / VaR(X)$

Take the nth scenario,

corresponding to the

selected alpha

percentile



DDEM NATCAT

5 - VaR HD Approach in practice

Basically, the VaR_HD is an estimator of the VaR, which consist in a weighted average using the "HD weights"

 $\Phi_{i} = VaR_{HD}(X_{i}) /$

 $VaR_HD(X)$

				L L	REDI		FREM	INU	NCAT	FREIMINATCAT		
	Base Sce	nario	o Total	Base Sc	enario	I	Base Sc	enar	io	Base Sc	enario)
	MC_9	-1	,770,874	MC_9	-	82,055	MC_9	-	330,367	MC_9	-	12,234
	MC_31	-1	,232,559	MC_31	-	65,327	MC_31	-	213,586	MC_31	-	26,133
	MC_42	-	780,867	MC_42	-	31,870	MC_42		109,577	MC_42	-	80,510
	MC_26	-	769,784	MC_26		1,587	MC_26	-	179,759	MC_26		15,845
	MC_17	-	620,535	MC_17	-	12,189	MC_17	-	103,331	MC_17	-	578
	MC_6	-	573,607	MC_6	-	13,173	MC_6		147,894	MC_6	-	48,744
	MC_30	-	554,017	MC_30	-	- 38 <mark>1</mark>	MC_30	-	106,315	MC_30		15,249
	MC_38	-	420,353	MC_38		4,539	MC_38	-	15,992	MC_38	-	14,597
	MC_1	-	389,383	MC_1	-	2,349	MC_1	-	284,997	MC_1	-	24,394
	MC_11	-	371,803	MC_11	-	13,17 <mark>8</mark>	MC_11	-	20,013	MC_11	-	30,749
	MC_19	-	352,858	MC_19		7,49 <mark>1</mark>	MC_19	-	201,352	MC_19		18,581
F	MC_10		291,491	MC_10		4,539	MC_10	-	390,677	MC_10		17,539
I	MC_23	-	289,611	MC_23	-	9,237	MC_23		128,032	MC_23	-	12,162
L	MC_48		238,699	MC_48		- 3,55 5-	MC_48		198,233	MC_40	-	7,398
	MC_8	-	146,126	MC_8	-	3,338	MC_8		82,130	MC_8	-	30,636
	MC_32	-	142,095	MC_32		1,587	MC_32	-	253,176	MC_32	-	30,569
	MC_34	-	96,648	MC_34		1,587	MC_34	-	213,490	MC_34		11,117
	MC_44	-	58,980	MC_44		2,57 <mark>1</mark>	MC_44		126,183	MC_44	-	12,032
	ivic_22	-	24,103	MC_22	-	4,317	IVIC_22		213,096	MC_22	-	53,112
	MC_35	-	17,751	MC_35		3,555	MC_35		84,257	MC_35	-	6,160
	MC_29		10,713	MC_29		603	MC_29	-	234,246	MC_29	-	18,798

DDEM NONCAT

CDEDIT

 $VaR_HD(X) =$ E(X | selected scenarios)around VaR(X))

TOTAL

 $VaR_HD(X_i) =$ $E(X_i | \text{ selected scenarios})$ around VaR(X))

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5 - TVaR Approach in practice

Consider <i>p</i> (alpha	Т	OTAL	C	REDI	Т	PREM NONCAT		PREM NATCAT		
	Base Sce	enario Total	Base Scenario		Base Scenario		Base Sc	Base Scenario		
driven) scenarios	MC_9	-1,770,874	MC_9	-	82,055	MC_9	- 330,367	MC_9	-	12,234
	MC_31	-1,232,559	MC_31	-	65,327	MC_31	- 213,586	MC_31	-	26,133
	MC_42	- 780,867	MC_42	-	31,87D	MC_42	109,577	MC_42	-	80,510
	MC_26	- 769,784	MC_26		1,587	MC_26	- 179,759	MC_26		15,845
+	MC_17	- 620,535	MC_17	-	12,189	MC_17	- 103,331	MC_17	-	578
	MC_6	- 573,607	MC_6	-	13,17 <mark>8</mark>	MC_6	147 ,894	MC_6	-	48,744
Calculate expected	MC_30	- 554,817	MC_30	-	381	MC_30	- 106,315	MC_30		15,249
	MC_38	- 420,353	MC_38		4,539	MC_38	- 15,992	MC_38	-	14,597
values on selected	MC_1	- 389,383	MC_1	-	2,349	MC_1	- 284,997	MC_1	-	24,394
	MC_11	- 371,803	MC_11	-	13,178	MC_11	- 20,013	MC_11	-	30,749
scenarios	MC_19	- 352,858	MC_19		7,491	MC_19	- 201,352	MC_19		18,581
	MC_10	- 291,491	MC_10		4,539	MC_10	- 390,677	MC_10		17,539
	MC_23	- 289,611	MC_23	-	9,237	MC_23	128,032	MC_23	-	12,162
	MC_4U	- 230,699	MC_4U		3,555	MC_4U	190,233	MC_4U	-	7,398
$TV_{\alpha}P(X) = \frac{TVaR}{\sum X_i}$	MC_8	- 146,126		-	3,335	MC_8	82,130	MC_8	-	30,636
$\frac{IVaR(X)}{i} = \frac{1}{i} = \frac{1}{i}$	MC_32	- 142,095	MC_32		1,587	MC_32	- 253,176	MC_32	-	30,569
TVaR(X) $TVaR(X)$	MC_34	- 96,648	MC_34		1,587	MC_34	- 213,490	MC_34		11,117
	MC_44	- 58,980	MC_44		2,571	MC_44	126,183	MC_44	-	12,032
$\sum T V a R(X)$	MC_22	- 24,103		-	4,317	MC_22	213,096	MC_22	-	53,112
\sum_{i} i van (\mathbf{n}_{i})	IVIC_35	- 17,751			3,550	MC_35	04,257	MC 35	-	10,100
$=\frac{1}{TV_{\alpha}P(Y)}$	IVIC_29	10,713	IMIC_29		603	- MC_29	- 234,246	WC_29	-	10,790
$I V u \Lambda(\Lambda)$	-	$TV_{a}R(X)$	_			-		_		
$\Psi_{i} = I VaR(X_{i}) / I VaR(X)$	$E(X \text{ selected scenarios})$ $E(X_i \text{ selected scenarios})$						os)			



5 - Reallocation in Practice - Working Example



Foglio di lavoro di Microsoft Excel



5 - Reallocation in Practice - comments

CONs of the Methodolo	CONs of the Methodologies described							
Covariance Approach	Ok if we are restricted to a low number of sims, but we are not looking to the tails of the distribution, and therefore we could underestimate the RC reallocated to fat tailed marginals							
Decomp VaR Approach	Too much volatility in the allocation, this method is not reliable							
VaR HD Approach	Decent allocation method if we want to use the VaR for the total RC, but can show undesired effects (e.g. the diversifying allocation property is not always valid, especially for fat tailed distributions)							
TVaR Approach	No cons? ©							



Contents

- 1 Introduction
- 2 P&C Insurance Risks
 - I. Reserve Risk
 - II. Premium Risk

3 How to add value to business

- I. Reinsurance Optimization
- II. Risk Capital Allocation
- III. Risk Based Pricing





Opportunity cost = **RISK FREE INCOME** - **COST OF RISK CAPITAL (CoC)**

...so the idea is to rewrite the formula, taking into account also risk based opportunity cost with both interest income and cost of capital...



Let's consider one example

Product A

- Observed CoR 95%
- Profit from investments 2%
- Allocated CoC 1%

Technical Profit: 5% With Financial Profit: 7% With CoC: 6% **Product B**

- Observed CoR 90%
- Profit from investments 2%
- Allocated CoC 15%

Technical Profit: 10% With Financial Profit: 12% With CoC: -3%

Product B, even it seems more profitable than Product A, in practice lead the company to a loss



We get an EVA based approach:

$$EVA_{net} = \operatorname{Prem}_{net} - \operatorname{Losses}_{net} - \operatorname{Expenses}_{net} - \operatorname{CoC}_{net} + \operatorname{RF}_{net}$$

Underlining the Reinsurance EVA, a risk-based measure of the profitability of the reinsurance, we get:

$$EVA_{net} = \operatorname{Prem}_{gross} - \operatorname{Losses}_{gross} - \operatorname{Exp}_{gross} - \operatorname{CoC}_{gross} + \operatorname{RF}_{gross} + \operatorname{Reinsurance}_{EVA}$$

Where:

$$Reinsurance_{EVA} = Losses_{ceded} + Comm + CoC_{released} - Prem_{ceded} - RF_{ceded}$$



If we divide the previous formula by the Gross Earned Premiums, we obtain:

$$\frac{EVA_{net}}{Prem_{gross}} = 1 - LoR_{gross} - ExR_{gross} - CoC_Ratio_{gross} + RF_Ratio_{gross} + Reinsurance_Ratio_{EVA}$$

Defined all quantities as function of the Gross LoR and given a net profit level, our aim is to find the target Gross LoR (via goal seek) that makes the equation go to zero:

$$1 - \mathbf{LoR}_{gross} - \widehat{\text{profit}}_{net} - \widehat{\text{ExR}}_{gross} - \left[\text{CoC}_{\text{Ratio}_{gross}} + \text{RF}_{\text{Ratio}_{gross}} + \text{Reinsurance}_{\text{Ratio}_{EVA}} + \right] \rightarrow 0$$

Function(*LoR*)

In this way, setting for example the profit = 0, we get a "break even" CoR, that could help in business steering



An example of application (no reinsurance):

Product A (Property Non-Cat)

- Profit ratio set at 5%
- Rf ratio set at 2%
- CoC ratio set as 1%

Traditional View

Target CoR: 95% (97% if we consider financial result)

Economic View

Target CoR: 95% + 2% (Rf) -1% (CoC) = 96% Product B (Property w/Cat)

- Profit ratio set at 5%
- Rf ratio set at 2%
- CoC ratio set as 10%

Traditional View

Target CoR: 95% (97% if we consider financial result)

Economic View

Target CoR: 95% + 2% (Rf) -10% (CoC) = 87%

Even if the product seem similar from a technical perspective, on an economic basis they lead to different conclusions; also Reinsurance could be used strategically!



Taking again the EVA formula ...

 $1 - \mathbf{LoR}_{gross} - \widehat{\mathbf{profit}}_{net} - \widehat{\mathbf{ExR}}_{gross} - \mathbf{CoC}_{Ratio}_{gross} + \mathbf{RF}_{Ratio}_{gross} + \mathbf{Reinsurance}_{Ratio}_{EVA} \rightarrow 0$

- Net profit ratio is set by the pricing department
- Expense ratio is set by the pricing department, in order to match pure premium with the assumptions on losses used by the pricing models
- RF ratio quite easy to estimate, based on cash-flow projection of losses and curve rate assumption (that are given inputs)
- Reinsurance EVA ratio it's similar (as logic) to the EVA for the insurer and we link it to RIO results / outputs (another presentation on the topic? ③)
- At the moment, we have not explicitly considered the CoC released by the reinsurance (embedded in the CoC net)

In the next section we will focus on how we derive directly the <u>net</u> CoC Ratio



how to set the capital charge?	
STEP 1. RC allocation per LoB	STEP 2. Pricing Estimate
 Done for business monitoring, quarterly reporting Volume measures are: technical provisions and planned premiums Losses (i.e. Reserves) have a "Retrospective view" 	 Done during design of new products Volume measures are: planned losses (i.e. LoR) and planned premiums Focus on a single (future) CY Market Risks out of scope
Determines the RC charges per Premium and Reserves units	RC charges should be coherent with the "Retrospective view"

In this way, we are assuming that new products will have underlying portfolios



STEP 1. RC allocation per LoB

We perform the following steps:





STEP 1. RC allocation per LoB => INTRA-RISK allocation

The aim is to assign the risk allocations to each risk type. Many methods could be chosen:

- **1. TVaR** allocation @99%
- 2. Covariance allocation
- 3. Proportional method
- 4. Etc.

Everything depends on the model resolution, i.e. on how we derive the Capital Requirements (for example the Standard Formula don't allow a TVaR allocation)



STEP 1. RC allocation per LoB => INTRA-LoB allocation

The aim is to assign the risk allocations to each LoB.

			Ν	IAR KET + CR RISK	CAT RISK	TERROR RISK	PREMIUM RISK	RESERVE RISK	BUSINESS RISK	OP RISK
	Standal	one Risk		2,774,534	286,687	144,617	4,202,680	2,998,509	438,151	531,152
	Method	1		59.22%	19.96%	12.48%	33.27%	49.90%	23.36%	89.29%
LoB Name	Method	2,、		60.00%	60.00%	60.00%	60.00%	60.00%	60.00%	60.00%
PRODUCT 1	1	521,878		164,307	6,867	3,608	1 39,810	149,626	10,236	47,424
PRODUCT 2	1	263,713	N.	82,153	8,011	-	69,905	74,813	5,118	23,712
PRODUCT 3	<u>i</u> –	929,335	N.	377,905	4,578	3,608	83,886	344,140	6,142	109,076
PRODUCT 4		1,460,153		558,643	2,861	3,608	209,715	508,729	15,354	161,243
PRODUCT 5		537,087	1	65,723	12,017	5,412	349,524	59,850	25,591	18,970
PRODUCT 6	N. Start	524,345		98,584	7,439	-	279,619	89,776	20,472	28,455
PRODUCT 7	- N	952,785	1	295,752	15,450	1,804	265,638	269,327	19,449	85,364

... and we are able to allocate the quarterly RC for monitoring / reporting purpose!!



STEP 1. RC allocation per LoB => RC Charges per Premium and Reserve Unit

Finally we get the risk capital charges, per Premium and Reserve (gross of reinsurance) units, depending on risk types

LoB Name	/ Reserve	/ Premium	/ Premium	/ Premium	/ Reserve	/ Reserve	/ Reserve
PRODUCT 1	39%	0.92%	0.48%	18.63%	35.27%	2.41%	11.18%
PRODUCT 2	43%	2.18%	0.00%	18.99%	39.35%	2.69%	12.47%
PRODUCT 3	232%	0.58%	0.45%	10.58%	211.68%	3.78%	67.09%
PRODUCT 4	54%	0.27%	0.34%	19.47%	48.89%	1.48%	15.50%
PRODUCT 5	1%	0.28%	0.13%	8.26%	0.85%	0.36%	0.27%
PRODUCT 6	2%	1.24%	0.00%	46.59%	2.25%	0.51%	0.71%
PRODUCT 7	27%	3.23%	0.38%	55.52%	24.18%	1.75%	7.66%

MARKET + CR RISK CAT RISK TERROR RISK PREMIUM RISK RESERVE RISK BUSINESS RISK OP RISK

Given those, we need additional portfolio run-off assumptions to derive the whole Cost of Capital related to the product



STEP 2. Pricing Estimate

- evaluation in t=0
- all the premiums earned only in t=0+ (no unearned premium reserves set)
- business runs off until the end of payments
- market risks out of scope



> Premium risk arises only in t=0, due to the planning u/w for the period [0,1]

> Reserve risk arises for all futures times (t=1 to t=n-1), until the full run-off of the

reserve in *t=n*

> Business and Operational Risks rise until complete run-off



STEP 2. Pricing Estimate

We project future reserves (using a DY pattern) We apply the capital charges estimated at STEP (1)

SOLVENCY 2	Proxy of the run-off					
Technical Provisions	<i>t</i> = 0	1		2	3	4
BE	57.26%		23.86%	3.40%	1.05%	
NET CoC RATIO (MVM)	2.70%		1.13%	0.16%	0.05%	
LOSS TECHNICAL PROV	59.97%		24.98%	3.56%	1.10%	

Capital Requirement

Market + Credit Risk	24.75%	10.31% 1.47% 0.45%
Premium Risk Nat-Cat	2.18%	0.00% 0.00% 0.00%
Premium Risk Terror	0.00%	0.00% 0.00% 0.00%
Premium Risk Non-Cat	18.99%	0.00% 0.00% 0.00%
Reserve Risk	0.00%	9.39% 1.34% 0.41%
Business Risk	1.54%	0.64% 0.09% 0.03%
Operational Risk	7.14%	2.98% 0.42% 0.13%
	29.85%	13.01% 1.85% 0.57%



PROs	
1. Immediate reconciliation with quarterly reporting	\checkmark
2. Easy to make sensitivity analyses, especially on diversification	\checkmark
3. Being all explicit, it's easy to communicate with other departments, in particular for risk explanation	\checkmark

CONs	
1. Reserve Risk implicitly allows for diversification within AYs, but it makes sense if we consider a new product for an existing portfolio	\mathbf{X}

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Conclusion



"Ora, la forma dell'operazione militare è come quella dell'acqua. L'acqua, quando scorre, fugge le altezze e precipita verso il basso. L'operazione militare vittoriosa evita il pieno e colpisce il vuoto. Come l'acqua adegua il suo movimento al terreno, La vittoria in guerra si consegue adattandosi al nemico. L'abile condottiero non segue uno **shih** prestabilito e non mantiene una forma immutabile.

Modificare la propria tattica adattandosi al nemico è ciò che si intende per 'divino'."

Thank you for your attention.





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No duty to update

The company assumes no obligation to update any information contained herein.



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